

**MODEL PAPER - 6**

**MATHEMATICS**

1. If  $z = \frac{1-i\sqrt{3}}{1+i\sqrt{3}}$ , then principal amplitude of z is (Complex Numbers)
- 1)  $\frac{-2\pi}{3}$                       2)  $\frac{-\pi}{3}$                       3)  $\frac{\pi}{3}$                       4)  $\frac{2\pi}{3}$
2.  $\lim_{\alpha \rightarrow \beta} \frac{\sin^2 \alpha - \sin^2 \beta}{\alpha^2 - \beta^2}$  is equal to (Limits)
- 1) 0                      2) 1                      3)  $\frac{\sin \beta}{\beta}$                       4)  $\frac{\sin 2\beta}{2\beta}$
3. If  $x = \exp \left\{ \tan^{-1} \left( \frac{y-x^2}{x^2} \right) \right\}$ , then  $\frac{dy}{dx} =$  (Differentiation)
- 1)  $2x[1 + \tan(\log x)] + \sec^2(\log x)$                       2)  $x[1 + \tan(\log x)] + \sec^2(\log x)$   
 3)  $2x[1 + \tan(\log x)] + x^2 \sec^2(\log x)$                       4)  $2x[1 + \tan(\log x)] + x \sec^2(\log x)$
4. The denominator of a function is greater than 16 of the square of the numerator, then least value of the function is (Differentiation)
- 1)  $\frac{-1}{4}$                       2)  $\frac{-1}{8}$                       3)  $\frac{1}{\sqrt{2}}$                       4)  $\frac{1}{16}$
5. If  $\int f(x) \cos x \, dx = \frac{1}{2} f^2(x) + c$ , then f(x) can be (Integration)
- 1) x                      2) 1                      3) cos x                      4) sin x
6. The parabolas  $y^2 = 4x$  and  $x^2 = 4y$  divide the square region bounded by the lines  $x = 4$ ,  $y = 4$  and the coordinate axes into three parts  $s_1, s_2, s_3$  numbered from top to bottom. If  $s_1, s_2, s_3$  represent the areas of the above parts, then  $s_1 : s_2 : s_3$  equals (Parabola)
- 1) 1 : 1 : 1                      2) 2 : 1 : 2                      3) 1 : 2 : 3                      4) 1 : 2 : 1
7.  $(1^2) + (1^2 + 2^2) + (1^2 + 2^2 + 3^2) + \dots + n$  brackets = (Mathematical Induction)
- 1)  $\frac{n(n+1)(n+2)}{6}$                       2)  $\frac{n(n+1)^2(n+2)}{12}$                       3)  $\frac{n(n+1)(n+2)^2}{4}$                       4)  $\frac{n(n+1)(2n+1)}{6}$
8.  $f(x) = \begin{cases} -1, & -2 \leq x \leq 0 \\ x-1, & 0 < x \leq 2 \end{cases}$  then  $\{x \in [-2, 2] ; x \geq 0 : |f(x)| = x\} =$  (Functions)
- 1) {0}                      2)  $\left\{ \frac{1}{2} \right\}$                       3) {1}                      4)  $\phi$
9. Let  $f: (-1, 1) \rightarrow B$  be a function defined by  $f(x) = \tan^{-1} \left( \frac{2x}{1-x^2} \right)$  then f is both one one and onto when B is the interval (Functions)
- 1)  $\left( 0, \frac{\pi}{2} \right)$                       2)  $\left[ 0, \frac{\pi}{2} \right)$                       3)  $\left( -\frac{\pi}{2}, \frac{\pi}{2} \right)$                       4)  $\left[ -\frac{\pi}{2}, \frac{\pi}{2} \right]$
10. The position vectors of the points A, B, C are  $\bar{i} + \bar{j} + \bar{k}$ ,  $\bar{i} + 5\bar{j} - \bar{k}$  and  $2\bar{i} + 3\bar{j} + 5\bar{k}$  respectively the greatest angle of  $\Delta ABC$  is (Vectors)
- 1)  $90^\circ$                       2)  $135^\circ$                       3)  $120^\circ$                       4)  $\cos^{-1} \left( \frac{5}{7} \right)$
11. Vector equation of perpendicular bisector of  $A(\bar{a})$  and  $B(\bar{b})$  is (Vectors)
- 1)  $\bar{r} = (1-t)\bar{a} + t\bar{b}$                       2)  $\bar{r} = \bar{a} + t\bar{b}$                       3)  $\left( \bar{r} - \frac{\bar{a} + \bar{b}}{2} \right) \cdot (\bar{a} - \bar{b}) = 0$                       4)  $\left( \bar{r} - \frac{\bar{a} - \bar{b}}{2} \right) \cdot (\bar{a} + \bar{b}) = 0$

12. Length of perpendicular from the origin to the plane passing through the point A( $\vec{a}$ ) and containing the line  $\vec{r} = \vec{b} + \lambda\vec{c}$  is (Vectors)

1)  $\frac{[\vec{a} \vec{b} \vec{c}]}{|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}|}$     2)  $\frac{[\vec{a} \vec{b} \vec{c}]}{|\vec{a} \times \vec{b} + \vec{b} \times \vec{c}|}$     3)  $\frac{[\vec{a} \vec{b} \vec{c}]}{|\vec{b} \times \vec{c} + \vec{c} \times \vec{a}|}$     4)  $\frac{[\vec{a} \vec{b} \vec{c}]}{|\vec{c} \times \vec{a} + \vec{a} \times \vec{b}|}$

13. Volume of the tetrahedron with edges  $\vec{i} + 2\vec{j} + 2\vec{k}$ ,  $2\vec{i} - \vec{j} + 2\vec{k}$ ,  $2\vec{i} + 2\vec{j} - \vec{k}$ . (Vectors)

1)  $\frac{9}{2}$  cubic units    2)  $\frac{7}{2}$  cubic units    3)  $\frac{10}{2}$  cubic units    4)  $\frac{13}{2}$  cubic units

14. **Assertion (A):** For any vector  $\vec{a}$ ,  $|\vec{a} \times \vec{i}|^2 + |\vec{a} \times \vec{j}|^2 + |\vec{a} \times \vec{k}|^2 = 2|\vec{a}|^2$ . (Vectors)

**Reason (R):** For any vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ ,  $[\vec{a} \vec{b} \vec{c}] = (\vec{a} \times \vec{b}) \cdot \vec{c}$

Then the correct statement is

- 1) Both **A** and **R** are true and **R** is the correct explanation of **A**  
 2) Both **A** and **R** are true and **R** is not the correct explanation of **A**  
 3) **A** is true and **R** is false    4) **A** is false and **R** is true

15.  $\vec{a} = 2\vec{i} - 3\vec{j}$ ,  $\vec{b} = \vec{i} + \vec{j} - \vec{k}$ ,  $\vec{c} = 3\vec{i} - \vec{k}$ . (Vectors)

Match the following

**List - I**

**List II**

- i)  $[\vec{a} \vec{b} \vec{c}]$     a)  $\frac{2}{3}$   
 ii)  $[\vec{b} + \vec{c} \quad \vec{c} + \vec{a} \quad \vec{a} + \vec{b}]$     b) 16  
 iii)  $[\vec{b} \times \vec{c} \quad \vec{c} \times \vec{a} \quad \vec{a} \times \vec{b}]$     c) 8  
 iv) Volume of the tetrahedron with  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  as coterminal edges is    d) 4

The correct match from list I to II is

- 1) d, c, b, a    2) b, c, a, d    3) c, d, a, b    4) d, b, c, a

16.  $A = [a_{ij}]_{n \times n}$  such that  $a_{ij} = (i + j)^2$  and trace of  $A = 120$  then  $n =$  (Matrices)
- 1) 3    2) 6    3) 5    4) 4

17. If  $n \in \mathbb{Z}$ , the value of  $\begin{vmatrix} n^2 & (n+1)^2 & (n+2)^2 \\ (n+3)^2 & (n+4)^2 & (n+5)^2 \\ (n+6)^2 & (n+7)^2 & (n+8)^2 \end{vmatrix}$  is (Matrices)
- 1) - 8    2) 8    3) - 216    4) - 108

18. The system of  $n$  equations in ' $n$ ' unknowns expressed in the form of  $AX = B$  has infinitely many solutions if (Matrices)
- 1)  $|A| \neq 0$     2)  $|A| \neq 0, (\text{adj } A) B \neq O$     3)  $|A| = 0, (\text{adj } A) B = O$     4)  $|A| \neq 0, (\text{adj } A) B = O$

19. The value of  $\sqrt{1 - \cos^2 100^\circ} \cdot \text{cosec } 100^\circ + \sqrt{1 - \sin^2 100^\circ} \cdot \text{sec } 100^\circ =$  (Trigonometry)
- 1) 0    2) 2    3) 1    4) -2

20. If  $3 \sec \alpha - 5 \tan \alpha = k$ ,  $6 \sec \alpha + k \tan \alpha = 5$  then  $k^2 =$  (Trigonometry)
- 1) 34    2) 70    3) 14    4) 20

21. If  $\sin 2\theta = k$  then  $\frac{\tan^3 \theta}{1 + \tan^2 \theta} + \frac{\cot^3 \theta}{1 + \cot^2 \theta} =$  (Trigonometry)

1)  $\frac{1 - k^2}{k}$     2)  $\frac{2 - k^2}{k}$     3)  $\frac{1 + k^2}{k}$     4)  $\frac{2 + k^2}{k}$

22. Period of  $\sin \frac{\pi x}{2} + 2 \cos \frac{\pi x}{3} - \tan \frac{\pi x}{4}$  is (Trigonometry)

1) 12    2) 24    3) 16    4) 15

23.  $\sin \frac{\pi}{5} \sin \frac{2\pi}{5} \sin \frac{3\pi}{5} \sin \frac{4\pi}{5} =$  (Trigonometry)

1)  $\frac{2}{16}$     2)  $\frac{1}{16}$     3)  $\frac{3}{16}$     4)  $\frac{5}{16}$

24. The number of solutions of the equation  $\cot^2 x - (\sqrt{3} + 1)\cot x + \sqrt{3} = 0$  in the interval  $\left(0, \frac{\pi}{2}\right)$  (Trigonometry Equation)  
 1) 2                                      2) 3                                      3) 4                                      4) 0
25. The value of  $\tan\left(2\tan^{-1}\frac{1}{5} - \frac{\pi}{4}\right) =$  (Inverse Trigonometry)  
 1)  $\frac{7}{17}$                                       2)  $-\frac{5}{17}$                                       3)  $\frac{5}{17}$                                       4)  $-\frac{7}{17}$
26. If  $\sin \alpha \cos \beta = \cos \theta$  and  $\cos \alpha \sin \beta = \sin \theta$  then  $\sin^2 \beta =$  (Hyperbolic Function)  
 1)  $\cos \alpha$                                       2)  $\cos^2 \alpha$                                       3)  $\sin \alpha$                                       4)  $\sin^2 \alpha$
27. In  $\Delta ABC$ , if  $2a^2 + 4b^2 + c^2 = 4ab + 2ac$  then  $\cos B =$  (Properties of Triangle)  
 1)  $\frac{7}{8}$                                       2)  $\frac{5}{8}$                                       3)  $\frac{3}{8}$                                       4)  $\frac{1}{8}$
28. In  $\Delta ABC$ , if  $\frac{s-a}{11} = \frac{s-b}{12} = \frac{s-c}{13}$  then  $\tan^2 \frac{A}{2} =$  (Properties of Triangle)  
 1)  $\frac{11}{39}$                                       2)  $\frac{13}{33}$                                       3)  $\frac{12}{37}$                                       4)  $\frac{33}{13}$
29. In  $\Delta ABC$ ,  $r_1 = 2r_2 = 3r_3$  then  $\angle A =$  (Properties of Triangle)  
 1)  $\frac{\pi}{3}$                                       2)  $\frac{\pi}{4}$                                       3)  $\frac{\pi}{2}$                                       4)  $\frac{2\pi}{3}$
30. Sum of 99<sup>th</sup> powers of the roots of the equation  $x^7 - 1 = 0$  is (De-Moiver's Theroem)  
 1) 0                                      2) 99                                      3) -99                                      4) 693
31. **Statement I:**  $x^2 - 2x + 10$  has minimum value at  $x = 1$  (Quadratic expression)  
**Statement II:**  $2x - 7 - 5x^2$  has maximum value at  $x = 1$   
 1) Only I is true                                      2) Only II is true                                      3) Both I and II are true                                      4) Neither I nor II is true
32.  $\sec \alpha, \operatorname{cosec} \alpha$  are roots of  $x^2 - px + q = 0$  then (Quadratic expression)  
 1)  $p^2 = q(q - 2)$                                       2)  $p^2 = q(q + 2)$                                       3)  $p^2 + q^2 = 2q$                                       4)  $p^2 + q^2 = 2p$
33.  $\alpha, \beta, \gamma$  are roots of the equation  $x^3 - 3x + 1 = 0$  then the equation whose roots are  $\alpha - \frac{1}{\beta\gamma}, \beta - \frac{1}{\gamma\alpha}, \gamma - \frac{1}{\alpha\beta}$  (Theory expression)  
 1)  $x^3 - 3x + 8 = 0$                                       2)  $x^3 - 12x + 8 = 0$                                       3)  $x^3 - 6x + 8 = 0$                                       4)  $x^3 - 9x + 8 = 0$
34. Exponent of 7 in  $100!$  is (Permutaion & Combination)  
 1) 97                                      2) 24                                      3) 14                                      4) 16
35. There are 3 different books on economics, 4 different books on political science and 5 different books on geography. Total number of selections with atleast one book on each subject is (Permutaion & Combination)  
 1) 4095                                      2) 4096                                      3) 3255                                      4) 3254
36. The term independent of  $x$  in the expansion of  $\left(\frac{2\sqrt{x}}{5} - \frac{1}{2x\sqrt{x}}\right)^{11}$  is (Binomial Theorem)  
 1) 8<sup>th</sup> term                                      2) 6<sup>th</sup> term                                      3) 5<sup>th</sup> term                                      4) does not exist
37. If  $C_r$  stands for  ${}^nC_r$  and  $\sum_{r=1}^n r \cdot \frac{C_r}{C_{r-1}} = 210$  then  $n =$  (Binomial Theorem)  
 1) 19                                      2) 20                                      3) 21                                      4) 10
38. If  $\frac{3x^3 - 8x^2 + 10}{(x-1)^4} = \frac{A}{x-1} + \frac{B}{(x-1)^2} + \frac{C}{(x-1)^3} + \frac{D}{(x-1)^4}$ , then the descending order of A, B, C, D is (Partial Fractions)  
 1) C, B, A, D                                      2) D, A, C, B                                      3) D, B, A, C                                      4) D, A, B, C
39. Variance of 20 observations is 5. If each observations is increased by 2, the variance of the resulting observations is (Measure of Dispersion)  
 1) 0.2                                      2) 5                                      3) 10                                      4) 20
40. A team of 8 couples (husband and wife) attend a lucky draw in which 4 persons picked up for a prize. Then the probability that there is atleast one couple is (Probability)  
 1)  $\frac{11}{39}$                                       2)  $\frac{8}{13}$                                       3)  $\frac{5}{13}$                                       4)  $\frac{14}{39}$
41. Two numbers are selected randomly from the set  $S = \{1, 2, 3, 4, 5, 6\}$  without replacement one by one. The probability that minimum of the two numbers is less than 4 is (Probability)  
 1)  $\frac{1}{15}$                                       2)  $\frac{1}{5}$                                       3)  $\frac{4}{5}$                                       4)  $\frac{3}{5}$

42. Three numbers are chosen at random without replacement from  $\{1, 2, 3, \dots, 10\}$ . The probability that minimum of the chosen numbers is 3 or their maximum is 7 is **(Probability)**  
 1)  $\frac{11}{30}$                       2)  $\frac{11}{40}$                       3)  $\frac{13}{40}$                       4)  $\frac{1}{7}$
43. X follows a binomial distribution with parameters  $n = 8$  and  $p = \frac{1}{2}$  then  $P(|X - 4| \leq 2) =$  **(Random Variables)**  
 1)  $\frac{118}{128}$                       2)  $\frac{119}{128}$                       3)  $\frac{117}{128}$                       4)  $\frac{121}{128}$
44. A person who throws a die gains two points for getting an even number and loses one point for getting an odd number. If 4 dice are rolled and total score X is observed then the range of X is **(Random Variables)**  
 1)  $\{-4, 5, 8\}$                       2)  $\{-4, -1, 0, 5, 8\}$                       3)  $\{-4, -1, 2, 5, 8\}$                       4)  $\{-4, -2, -1, 2, 5, 8\}$
45. If the vertices P, Q, R of a triangle are rational points, which of the following points of the triangle PQR is always rational point? **(2D)**  
 1) centroid                      2) incentre                      3) orthocentre                      4) circumcentre
46. The locus of the point of intersection of the lines  $x \sin \theta + (1 - \cos \theta) y = a \sin \theta$ ,  $x \sin \theta - (1 + \cos \theta) y + a \sin \theta = 0$  is **(Locus)**  
 1) parabola                      2) ellipse                      3) straight line                      4) circle
47. When origin is shifted to suitable point the equation  $xy + 3x - 4y = c$  transforming as  $XY = 10$  then  $c =$  **(Transformation of axis)**  
 1) 22                      2) -22                      3) 2                      4) -2
48. Each side of square is of length 4. The centre of the square is (3, 7) and one of its diagonals is parallel to  $y = x$ . Then the coordinates of its vertices are **(Straight Lines)**  
 1) (2, 5), (2, 7), (4, 7), (4, 4)                      2) (2, 5), (2, 6), (3, 5), (3, 6)  
 3) (1, 5), (1, 9), (5, 9), (5, 5)                      4) (1, 5), (1, 9), (4, 7), (4, 4)
49. The length of the perpendicular from the point (0, 0) to the straight line passing through P(1, 2) such that P bisects the intercepted portion between the axes is **(Straight Lines)**  
 1)  $\sqrt{5}$                       2)  $\frac{4}{\sqrt{5}}$                       3) 4                      4)  $\frac{\sqrt{5}}{4}$
50. If the acute angle between the lines  $2x - 3y + 1 = 0$ ,  $kx + 5y - 6 = 0$  is  $\frac{\pi}{4}$  then  $k =$  **(Straight Lines)**  
 1) 1                      2) 2                      3) -1                      4) -2
51. The centroid of the triangle formed by the lines  $x^2 + xy - 2y^2 = 0$ ,  $x + y + 2 = 0$  **(Pair of Straight Lines)**  
 1)  $\left(\frac{5}{3}, \frac{1}{3}\right)$                       2)  $\left(\frac{-5}{3}, \frac{1}{3}\right)$                       3)  $\left(\frac{5}{3}, \frac{-1}{3}\right)$                       4)  $\left(\frac{-5}{3}, \frac{-1}{3}\right)$
52. If  $y = mx$  bisects the angle between the lines  $x^2(\tan^2 \theta + \cos^2 \theta) + 2xy \tan \theta - y^2 \sin^2 \theta = 0$ . If  $\theta = \frac{\pi}{3}$ , the value of  $\sqrt{3} m^2 + 4m$  is **(Pair of Straight Lines)**  
 1) 1                      2)  $\frac{1}{\sqrt{3}}$                       3)  $\sqrt{3}$                       4)  $7\sqrt{3}$
53. If  $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$  represents a pair of parallel lines then  $\sqrt{\frac{g^2 - ac}{f^2 - bc}} =$  **(Pair of Straight Lines)**  
 1)  $\frac{a}{b}$                       2)  $\frac{b}{a}$                       3)  $\sqrt{\frac{b}{a}}$                       4)  $\sqrt{\frac{a}{b}}$
54. P, Q, R, S, T are five collinear points such that  $PQ = QR = RS = ST$  and  $P = (x_1, y_1, z_1)$  and  $T = (x_2, y_2, z_2)$  then the point  $\left(\frac{5x_2 + 3x_1}{8}, \frac{5y_2 + 3y_1}{8}, \frac{5z_2 + 3z_1}{8}\right)$  is midpoint of **(3D)**  
 1) PQ                      2) QR                      3) RS                      4) ST
55. The angle between the lines whose direction cosines are given by the equations  $3\ell + m + 5n = 0$  and  $6mn - 2\ell n + 5\ell m = 0$  is **(Direction Cosines)**  
 1)  $\text{Cos}^{-1}\left(\frac{1}{3}\right)$                       2)  $\text{Cos}^{-1}\left(\frac{1}{6}\right)$                       3)  $\text{Cos}^{-1}\left(\frac{2}{3}\right)$                       4)  $\text{Cos}^{-1}\left(\frac{5}{6}\right)$
56. The equation of the plane through the point (-1, 6, 2) and perpendicular to the planes  $x + 2y + 2z - 5 = 0$  and  $3x + 3y + 2z - 8 = 0$  is **(Plane)**  
 1)  $2x - 4y + 3z + 20 = 0$                       2)  $2x + y - 3z + 26 = 0$                       3)  $2x - 4y + 3z + 23 = 0$                       4)  $2x + 5y - 2z + 12 = 0$

57.  $\lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{x^4} =$  (Limits)  
 1)  $\frac{1}{2}$                       2)  $\frac{1}{4}$                       3)  $\frac{1}{8}$                       4)  $\frac{1}{16}$
58. If  $f(x)$  is continuous in  $[0, 1]$  and  $f\left(\frac{1}{3}\right) = 1$  then  $\lim_{n \rightarrow \infty} f\left(\frac{n}{\sqrt{9n^2 + 1}}\right) =$  (Continuous)  
 1) 1                      2) 0                      3)  $\frac{1}{3}$                       4) 2
59.  $f: \mathbb{R} \rightarrow \mathbb{R}$  is a function such that  $f(1) = 2$ ,  $f(2) = 6$ , and  $f(x+y) = f(x) + kxy - 2y^2$  for all  $x, y \in \mathbb{R}$  then (Functions)  
 1)  $f'(x) = f(x)$                       2)  $f'(x) = 6f(x)$                       3)  $f'(x) = 6$                       4)  $f'(x) = 6x$
60. The radius and height of a cylinder are equal to the radius of a sphere. The ratio of the rates of change of volumes of the sphere and cylinder respectively is (Rate of Changes)  
 1) 3 : 4                      2) 2 : 3                      3) 3 : 2                      4) 4 : 3
61. The tangent to the curve  $y = x^3 - 6x^2 + 9x + 4$ ,  $0 \leq x \leq 5$  has minimum slope at  $(x_1, y_1)$  then  $x_1 =$  (Tangents & Normals)  
 1) 2                      2) 3                      3) 4                      4) 5
62. The tangent drawn to the ellipse  $\frac{x^2}{64} + \frac{y^2}{49} = 1$  cuts the coordinate axes at A, B. Then least length of AB is (Ellipse)  
 1) 40                      2) 30                      3) 15                      4) 225
63. Semi vertical angle of a cone is  $45^\circ$ , and height is 30.05 cm, then which of the following are true? (Errors)  
**Statement I:** Error in volume is  $45\pi$ .  
**Statement II:** Percentage error in volume is  $\frac{1}{2}$ .  
 1) Only I                      2) Only II                      3) both I & II                      4) neither I nor II
64. The value of  $c$  for which the conclusion of mean value theorem holds for the function  $f(x) = \log_e x$  on the interval  $[1, 3]$  is (Mean Value Theorem)  
 1)  $\frac{1}{2} \log_e 3$                       2)  $2 \log_3 e$                       3)  $\log_3 e$                       4)  $\log_e 3$
65. If the relation between subnormal SN and subtangent ST at any point on the curve  $by^2 = (x + a)^3$  is  $p(\text{SN}) = q(\text{ST})^2$ , then  $\frac{p}{q} =$  (Tangents & Normals)  
 1)  $\frac{8b}{27}$                       2)  $\frac{27}{8b}$                       3)  $\frac{27b}{8}$                       4)  $\frac{8}{27b}$
66. **Assertion (A):** Both  $\sin x$  and  $\cos x$  are decreasing functions in the interval  $\left(\frac{\pi}{2}, \pi\right)$ . (Maxima & Minima)  
**Reason (R):** If a differentiable function decreases in an interval  $(a, b)$  then its derivative also decreases in  $(a, b)$ .  
 1) Both (A) and (R) are true and (R) is the correct explanation of (A)  
 2) Both (A) and (R) are true and (R) is not the correct explanation of (A)  
 3) (A) is true and (R) is false                      4) (A) is false and (R) is true
67. The length of the intercept cut by the circle  $x^2 + y^2 - 7x + 5y + 12 = 0$  on the x-axis is (Circles)  
 1) 3                      2) 1                      3) 4                      4) 2
68. The angle between the pair of tangents from  $(13, 0)$  to the circle  $x^2 + y^2 = 25$  is (Circles)  
 1)  $\cos^{-1}\left(\frac{5}{12}\right)$                       2)  $\tan^{-1}\left(\frac{5}{12}\right)$                       3)  $2\cos^{-1}\left(\frac{5}{12}\right)$                       4)  $2\tan^{-1}\left(\frac{5}{12}\right)$
69. The radical axis of two non-intersecting circles divides the line segment joining the centres of circles in the ratio (System of Circles)  
 1) of their areas                      2) of their radii                      3) 1 : 1                      4) 1 : -1
70. If the slopes of normals at  $P(8, 8)$ ,  $Q(2, -4)$ ,  $R(8, -8)$  on parabola  $y^2 = 8x$  are  $m_1, m_2, m_3$  then ascending order of  $m_1, m_2, m_3$  is (Parabola)  
 1)  $m_1, m_2, m_3$                       2)  $m_1, m_3, m_2$                       3)  $m_3, m_1, m_2$                       4)  $m_2, m_3, m_1$
71. The equation to the directrix of the parabola  $x^2 + 8x + 12y + 4 = 0$  is (Parabola)  
 1)  $x - 4 = 0$                       2)  $x + 4 = 0$                       3)  $y - 4 = 0$                       4)  $y + 4 = 0$
72. The latusrectum of an ellipse is  $\frac{1}{3}$  of the major axis. Its eccentricity is (Ellipse)  
 1)  $\frac{2}{3}$                       2)  $\sqrt{\frac{2}{3}}$                       3)  $\sqrt{\frac{3}{2}}$                       4)  $\frac{2}{\sqrt{3}}$

73. The equation to the director circle of the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  is (Ellipse)
- 1)  $x^2 + y^2 = 25$       2)  $x^2 + y^2 = 16$       3)  $x^2 + y^2 = 9$       4)  $x^2 + y^2 = 41$
74. If the line  $x + y + 1 = 0$  is an asymptote of  $x^2 - y^2 + x - y - 2 = 0$ , the other asymptote is (Hyperbola)
- 1)  $x + y = 0$       2)  $x - y = 0$       3)  $x - y = 1$       4)  $x - y + 1 = 0$
75.  $\int \frac{2x + \sin 2x}{1 + \cos 2x} dx =$  (Integration)
- 1)  $x \tan x + c$       2)  $x \sec x + c$       3)  $x \sec x \tan x + c$       4)  $x (\tan x + \sec x) + c$
76.  $\int_0^{\pi/2} \frac{4 \sin x + 3 \cos x}{\sin x + \cos x} dx =$  (Definite Integrals)
- 1)  $\frac{5\pi}{4}$       2)  $\frac{3\pi}{2}$       3)  $\frac{7\pi}{4}$       4)  $\frac{5\pi}{6}$
77.  $\int_0^{\pi/4} \frac{\sin x + \cos x}{3 + \sin 2x} dx =$  (Definite Integrals)
- 1)  $\log 2$       2)  $\log 3$       3)  $\frac{1}{4} \log 3$       4)  $\frac{1}{8} \log 3$
78. The area of the region bounded by  $|x| + |y| = 1$  is (Areas)
- 1) 1      2) 2      3)  $\sqrt{2}$       4)  $2\sqrt{2}$
79. The general solution  $\frac{dy}{dx} = \sqrt{1 - x^2 - y^2 + x^2 y^2}$  is (Differentiation Equations)
- 1)  $\sin^{-1} y = \frac{1}{2} \sin^{-1} x + c$       2)  $\sin^{-1} y = x \sqrt{1 - x^2} + \sin^{-1} x + c$
- 3)  $2 \sin^{-1} y = x \sqrt{1 - x^2} + \sin^{-1} x + c$       4)  $\sin^{-1} y = \sin^{-1} x + c$
80. An integrating factor of  $(x + y + 1) \frac{dy}{dx} = 1$  is (Differentiation Equations)
- 1)  $e^{-x}$       2)  $e^{-y}$       3)  $e^x$       4)  $e^y$