## MODEL PAPER - 7

## MATHEMATICS

1. If $f(x)=\left|\begin{array}{ccc}\sin x+\sin 2 x+\sin 3 x & \sin 2 x & \sin 3 x \\ 3+4 \sin x & 3 & 4 \sin x \\ 1+\sin x & \sin x & 1\end{array}\right|$, then the value of $\int_{0}^{\pi / 2} f(x) d x$ is
(Integration)
1) 3
2) $\frac{2}{3}$
3) $\frac{1}{3}$
4) 0
2. Let the function $f: R \rightarrow R$ be defined by $f(x)=2 x+\sin x, x \in R$. Then $f$ is
(Functions)
1) one - one and onto
2) one - one but not onto
3) onto but not one - one
4) neither one - one nor onto
3. The incentre of the triangle with vertices $(1, \sqrt{3}),(0,0)$ and $(2,0)$ is
(Straight Lines)
1) $\left(1, \frac{\sqrt{3}}{2}\right)$
2) $\left(1, \frac{1}{\sqrt{3}}\right)$
3) $\left(\frac{2}{3}, \frac{1}{\sqrt{3}}\right)$
4) $\left(\frac{2}{3}, \frac{\sqrt{3}}{2}\right)$
4. A hyperbola has the asymptotes $x+2 y=3$ and $x-y=0$ and passes through ( 2,1 ), its centre is (Hyperbola)
1) $(1,2)$
2) $(2,2)$
3) $(2,1)$
4) $(1,1)$
5. For $|x|<1$, let $y=1+x+x^{2}+$ $\qquad$ $\infty$, then $\frac{d y}{d x}-\mathbf{y}=$
(Differentiation )
1) $\frac{x}{y}$
2) $x y^{2}$
3) $\frac{x}{y^{2}}$
4) $\frac{x^{2}}{y^{2}}$
6. $\int(5+\log \sin x)^{2} \cdot \frac{\cos x}{\sin x} d x=$
(Integration)
1) $\int(5+\log \sin x)^{3}+c$
2) $\log \sin x+c$
3) $\frac{1}{3}\left(5+1 \circ^{\circ} g \sin x\right)^{3}+c$ 4) $\frac{-1}{3}(5+\log \sin x)^{3}+c$
7. The area bounded by $y=\log x, x$-axis and the ordinates $x=1, x=2$ is (in sq. units)
(Areas)
1) $\frac{1}{2}(\log 2)^{2}$
2) $\log \left(\frac{2}{e}\right)$
$3)^{\log \left(\frac{4}{e}\right)}$
3) $\log 4$
8. The standard deviation of $3,9,11,7,5$ is
(Measure of Dispersion)
1) $2 \sqrt{2}$
2) 2
3) $3 \sqrt{2}$
4) $2 \sqrt{3}$
9. The equation whose roots are $k$ times the roots of $x^{4}+2 a x^{3}+4 b x^{2}+8 a x+16=0$ is reciprocal equation, then $k=$
(Theory of Equations)
1) 2
2) 3
3) $\frac{1}{2}$
4) $\frac{1}{3}$
10. If $\alpha, \beta, \gamma$ are the roots of the equation $x^{3}-10 x^{2}+7 x+8=0$, then match the following: (Theory of Equations)
1) $\alpha+\beta+\gamma$
a) $-43 / 4$
2) $\alpha^{2}+\beta^{2}+\gamma^{2}$
b) $-7 / 8$
3) $\frac{1}{\alpha}+\frac{1}{\beta}+\frac{1}{\gamma}$
c) 86
4) $\frac{\alpha}{\beta \gamma}+\frac{\beta}{\gamma \alpha}+\frac{\gamma}{\alpha \beta}$
d) 0
e) 10

The correct match is

1) 1-e, 2-c, 3-a, 4-b
2) 1-d, 2-c, 3-a, 4-b
3) 1-e, 2-c, 3-b, 4-a
4) 1-e, 2-b, 3-c, 4-a
11. If $z=\cos \alpha+i \sin \alpha$, then the amplitude of $z^{2}+\bar{z}$ is
(Complex Numbers)
1) $\frac{\alpha}{2}$
2) $\alpha$
3) $\frac{3 a}{2}$
4) $2 \alpha$
12. If $\left|z_{1}-1\right|<1,\left|z_{2}-2\right|<2,\left|z_{3}-3\right|<3$ then $\left|z_{1}+z_{2}+z_{3}\right|=$
(Complex Numbers)
1 ) is less than 6
2) is less than 12
3 ) is less than 3
3) is less than 9
13. $\left(\frac{1+i \sqrt{3}}{1-i \sqrt{3}}\right)^{6}+\left(\frac{1-i \sqrt{3}}{1+i \sqrt{3}}\right)^{6}=$
$\qquad$ (De-Movier's Theorem)
1) -1
2) 0
3) 1
4) 2
14. Let $\alpha, \beta$ be the roots of the equation $(x-a)(x-b)=c, c \neq 0$. Then the roots of the equation $(x-\alpha)(x-\beta)+c=0$ are
1) a, c
2) b, c
3) $a, b$
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15. The value of $k$, for which the equation $x^{2}+2(k+1) x+k^{2}=0$ has equal roots, is
(Quadratic Expression)
1) -1
2) $-\frac{1}{2}$
3) 1
4) 2
16. If $R=(5 \sqrt{5}+11)^{2 n+1}, f=R-[R]$ then $R f=$
(Binomial Theorem)
1) 1
2) $2^{n}$
3) $2^{2 n}$
4) $4^{2 n+1}$
17. If $\frac{1}{(x-a)\left(x^{2}+b\right)}=\frac{A}{x-a}+\frac{B x+C}{x^{2}+b}$ then $B=$
(Partial Fraction)
1) $\frac{1}{a^{2}+b}$
2) $\frac{-1}{a^{2}+b}$
3) $\frac{1}{a+b^{2}}$
4) $-\frac{1}{a+b^{2}}$
18. The letters of the word RANDOM are written in all possible ways and these words written out as in a dictionary then the rank of the word RANDOM is
(Permutation \& Combination)
1) 614
2) 615
3) 613
4) 616
19. The number of rectangles on a chess board is
(Permutation \& Combination)
1) 1225
2) 1296
3) 900
4) 1024
20. The number of natural numbers less than 1000 are divisible by 5 in which no digit occurs more than once in the same number is
(Permutation \& Combination)
1) 154
2) 136
3) 144
4) 152
21. If $P(A \cup B)=\frac{3}{4} ; P(\bar{A})=\frac{2}{3}$ then $P(\bar{A} \cap B)=$
(Probability)
1) $\frac{1}{12}$
2) $\frac{7}{12}$
3) $\frac{5}{12}$
4) $\frac{11}{12}$
22. Seven chits are numbered 1 to 7 . Four are drawn one by one with replacement. The probability that the least number on any selected chit is 5 , is
(Probability)
1) $1-\left(\frac{2}{7}\right)^{4}$
2) $4\left(\frac{2}{7}\right)^{4}$
3) $\left(\frac{3}{7}\right)^{4}-\left(\frac{2}{7}\right)^{4}$
4) $\left(\frac{3}{7}\right)^{4}$
23. A bag contains four balls, two balls are drawn and found to be white. The probability that all the balls in bag are white is
(Probability)
1) $\frac{2}{5}$
2) $\frac{1}{5}$
3) $\frac{4}{5}$
4) $\frac{3}{5}$
24. A random variable $X$ has the following distribution
(Random Variables)

| $X=x_{i}:$ | 1 | 2 | 3 | 4 |
| :--- | :--- | ---: | ---: | ---: |
| $P\left(X-x_{i}\right):$ | $k$ | $2 k$ | $3 k$ | $4 k$ |

then $k, P(x<3)$

1) $\frac{1}{10}, \frac{3}{5}$
2) $\frac{1}{10}, \frac{3}{10}$
3) $\frac{3}{10}, \frac{1}{10}$
4) $\frac{1}{10}, \frac{5}{12}$
25. $X$ is a Poisson variate such that $P(X=2)=\frac{2}{3} P(X=1)$ then $P(X=0)=$
(Random Variables)
1) $e^{-\frac{3}{4}}$
2) $e^{-\frac{4}{3}}$
3) $e^{-\frac{1}{3}}$
4) $e^{\frac{1}{3}}$
26. The range of function $f(x)=4^{x}+2^{x}+4^{-x}+2^{-x}+3$ is
(Functions)
1) $\left[\frac{3}{4}, \infty\right)$
2) $\left(\frac{3}{4}, \infty\right)$
3) $(7, \infty)$
4) $[7, \infty)$
27. If the sum to $n$ terms of a series is $2^{n+1}+n-2$ then $n^{\text {th }}$ term $=$
(Mathematical Induction)
1) $3^{n}-1$
2) $2^{n}+1$
3) $2^{n}-1$
4) $3^{n}+1$
28. OABC is a parallelogram with $\overline{\mathrm{AB}}=\overline{\mathrm{a}}$ and $\overline{\mathrm{OB}}=\overline{\mathrm{b}}$ then $\overline{\mathrm{OA}}=$
(Vectors)
1) $\bar{a}+\bar{b}$
2) $\bar{a}-\bar{b}$
3) $\bar{b}-\bar{a}$
4) $\frac{1}{2}(\bar{a}-\bar{b})$
29. $\bar{a}, \bar{b}, \bar{c}$ are three non coplanar vectors such that $\bar{a}+\bar{b}+\bar{c}=\alpha \bar{d}$ and $\bar{b}+\bar{c}+\bar{d}=\beta \bar{a}$ then $\bar{a}+\bar{b}+\bar{c}+\bar{d}$ is equal to
1) $\overline{0}$
2) $\alpha \bar{a}$
3) $\beta \bar{b}$
4) $(\alpha+\beta) \bar{c}$
(Vectors)
30. If the vectors $c x \bar{i}-6 \bar{j}+3 \bar{k}, x \bar{i}+2 \bar{j}+2 c x \bar{k}$ make an obtuse angle with each other for all real values for $x$ then
1) $-\frac{4}{3}<c<0$
2) $0<c \leq \frac{4}{3}$
3) $0 \leq \mathrm{c} \leq 2$
4) $c<0$
(Vectors)
31. The volume of a parallelopiped constructed on the diagonals of the faces of a given parallelopiped is $m$ times, the volume of the given paralleopiped then $\mathrm{m}=$
(Vectors)
1) 1
2) 2
3) 3
4) 4
32. Assertion(A): The points $A, B, C$ and $D$ with position vectors $4 \bar{i}+5 \bar{j}+\bar{k},-\bar{j}-\bar{k}, 3 \bar{i}+9 \bar{j}+4 \bar{k}$ and

$$
4(-\bar{i}+\overline{\mathrm{j}}+\overline{\mathrm{k}}) \text { respectively are coplanar. }
$$

(Vectors)
Reason(R): The vectors $\overline{D A}, \overline{D B}, \overline{D C}$ are linearly independent.
Which of the following is true?
The true statements are:

1) Both (A) and (R) are true and (R) is the correct explanation of (A)
2) Both (A) and (R) are true and (R) is not the correct explanation of (A)
3) (A) is true and (R) is false
4) (A) is false and (R) is true
33. Let $\overline{\mathrm{a}}, \overline{\mathrm{b}}, \overline{\mathrm{c}}$ be mutually perpendicular unit vectors
(Vectors)
Statement I: $|\overline{\mathrm{a}}+\overline{\mathrm{b}}+\overline{\mathrm{c}}|=\sqrt{3}$
Statement II : $\bar{a}+\bar{b}+\bar{c}$ is equally inclined to $\overline{\mathrm{a}}, \overline{\mathrm{b}}, \overline{\mathrm{c}}$.
1) I and II are true
2) I and II are false
3) I is false and II is true 4) I is true and II is false
34. If $A=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ and $B=\lambda A=\left[\begin{array}{cc}a & b \\ c & a+b+c\end{array}\right]$ then
(Matrices)
1) $B$ is a null matrix
2) $B=A$
3) $B$ is an ofentity matrix
4) $B=2 A$
35. $\left|\begin{array}{ccc}a+b & c & b+c \\ a-b & c & 3 b+c \\ b+c & c & a+b\end{array}\right|$ is equal to
1) $a+2 b+2 c$
2) 0
3) $a+2 b+c$
4) $2(a+b+c)$
36. The element in the first row and third column of the inverse of the matrix $\left[\begin{array}{ccc}1 & 2 & -3 \\ 0 & 1 & 2 \\ 0 & 0 & 1\end{array}\right]$ is
(Matrices)
1)     - 2
2) 0
3) 1
4) 7
37. The system of equations $x+y+z=6, x+2 y+\lambda z=0, x+2 y+3 z=10$ has no solution, then
(Matrices)
1) $\lambda=3$
2) $\lambda=5$
3) $\lambda=-5$
4) $\lambda=6$
38. If $\operatorname{cosec} A+\cot A=\frac{11}{2}$, then $\tan A$ is
(Trignometry)
1) $\frac{21}{22}$
2) $\frac{15}{16}$
3) $\frac{44}{117}$
4) $\frac{117}{44}$
39. If $\sin x+\cos x=\frac{1}{5}, 0 \leq x \leq \pi$, then $\tan x$ is equal to
(Trignometry)
1) $\frac{4}{3}$
2) $-\frac{4}{3}$ or $-\frac{3}{4}$
3) $\frac{4}{5}$
4) $\frac{8}{15}$
40. If $\sin \theta$ is the geometric mean between $\sin \phi$ and $\cos \phi$, then $\cos 2 \theta$ is equal to
(Trignometry)
1) $2 \sin ^{2}\left(\frac{\pi}{4}-\phi\right)$
2) $2 \cos ^{2}\left(\frac{\pi}{4}-\phi\right)$
3) $2 \cos \left(\frac{\pi}{4}+\phi\right)$
4) $2 \sin ^{2}\left(\frac{\pi}{4}+\phi\right)$
41. The period of $f(x)=\sin ^{2}\left(\frac{\pi}{8}+\frac{x}{2}\right)-\sin ^{2}\left(\frac{\pi}{8}-\frac{x}{2}\right)$ is
(Trignometry)
1) $\frac{\pi}{4}$
2) $\pi$
3) $\frac{\pi}{2}$
4) $2 \pi$
42. If $\tan \left(\frac{\pi}{4}+\theta\right)+\tan \left(\frac{\pi}{4}-\theta\right)=4$, then $\theta=$
(Trignometry Equations)
1) $n \pi \pm \frac{\pi}{3}$
2) $n \pi \pm \frac{\pi}{6}$
3) $n \pi \pm \frac{\pi}{4}$
4) $n \pi \pm \frac{\pi}{5}$
43. If $\operatorname{Tan}^{-1} \frac{x+1}{x-1}+\operatorname{Tan}^{-1} \frac{x-1}{x}=\operatorname{Tan}^{-1}(-7)$, then $x=$
(Inverse Trignometry)
1) 1
2) 2
3) no solution
4) -2
44. If $2 \sinh ^{-1}\left(\frac{\mathrm{a}}{\sqrt{1-\mathrm{a}^{2}}}\right)=\log \left(\frac{1+\mathrm{x}}{1-\mathrm{x}}\right)$ then $\mathrm{x}=$
(Hyperbola)
1) $a$
2) -a
3) $\frac{1+a}{1-a}$
4) $\frac{1-a}{1+a}$
45. If in a triangle $A B C, \frac{b+c}{11}=\frac{c+a}{12}=\frac{a+b}{13}$, then $\cos A$ is equal to
(Properties of Triangle)
1) $\frac{1}{5}$
2) $\frac{5}{7}$
3) $\frac{19}{35}$
4) $\frac{13}{35}$
46. If $p_{1}, p_{2}, p_{3}$ are respectively the perpendiculars from the vertices of a triangle to the opposite sides, then $p_{1} p_{2} p_{3}=$
(Properties of Triangle)
1) $\frac{a^{2} b^{2} c^{2}}{R^{3}}$
2) $\frac{a^{2} b^{2} c^{2}}{4 R^{3}}$
3) $\frac{4 a^{2} b^{2} c^{2}}{R^{3}}$
4) $\frac{a^{2} b^{2} c^{2}}{8 R^{3}}$
47. In an obtuse angled traingle, circumcentre lies
(Properties of Triangle)
1) inside the triangle
2) outside the triangle
3) lies on one side
4) it cannot be decided
48. If $A=(4,0), B=(-4,0)$ are the two points and $|A P-P B|=4$, then the locus of $P$ is
(Locus)
1) $3 x^{2}-y^{2}=12$
2) $x^{2}-3 y^{2}=1$
3) $3 x^{2}+y^{2}=12$
4) $x^{2}+3 y^{2}=12$
49. The transformed equation of $4 x^{2}+9 y^{2}-8 x+36 y+4=0$ when the axes are translated to (1, -2 ) is $a X^{2}+b Y^{2}=c$. Then descending order of $a, b, c$ is
(Transformation of Axes)
1) $c, b, a$
2) $c, a, b$
3) $a, b, c$
4) $a, c, b$
50. The equation of the altitude from $A$ to $B C$ of the triangle with vertices $A(0,1), B(2,0), C(2,-2)$ is
(Straight Lines)
1) $x-1=0$
2) $x+y-1=0$
3) $y-1=0$
4) $y=0$
51. A straight line passes through the fixed point $\left(\frac{1}{k}, \frac{1}{k}\right)$. The sum of the reciprocals of its intercepts on the coordinate axes is
(Straight Lines)
1) $\frac{2}{k}$
2) $\frac{k}{2}$
3) 2
4) $k$
52. The equation to the pair of lines through the origin andforming an equilateral triangle with the line $2 x+3 y+5=0$ is
(Pair of Straight Lines)
1) $23 x^{2}-48 x y+3 y^{2}=0$
2) $23 x^{2}+48 x y-3 y^{2}=0$
3) $23 x^{2}+48 x y+3 y^{2}=0$
4) $23 x^{2}-48 x y-3 y^{2}=0$
53. The length of the intercept on the $x$-axis cutby the pair of lines $2 x^{2}+5 x y+3 y^{2}+6 x+7 y+1=0$ is
(Pair of Straight Lines)
1) $\sqrt{7}$
2) $2 \sqrt{7}$
3) $\frac{\sqrt{7}}{2}$
4) $\sqrt{2}$
54. $A, B, C$ are the projections of $P(5,-2,6)$ on the coordinate planes then the centroid of the $\triangle A B C$ is
(3D)
1) $(5,-2,6)$
2) $\left(\frac{5}{3},-\frac{2}{3}, 2\right)$
3) $\left(\frac{20}{3},-\frac{8}{3}, 8\right)$
4) $\left(\frac{10}{3},-\frac{4}{3}, 4\right)$
55. $A=(-2,3,4), B=(-4,4,6), C=(4,3,5), D=(0,1,2)$ then the projection of $\overline{A B}$ on $\overline{C D}$ is
1) $\frac{1}{\sqrt{29}}$
2) $\frac{3}{\sqrt{29}}$
3) $\frac{16}{\sqrt{29}}$
4) 0
56. The equation of the plane passing through $(1,-2,4),(3,-4,5)$ and perpendicular to $y z$ - plane is
(Plane)
1) $2 y+z=0$
2) $y+2 z+6=0$
3) $y+2 z-6=0$
4) $3 y+2 z-2=0$
57. The equation of the circle of radius 5 with centre on $X$-axis and passing through the point ( 2,3 ) is (Circles) 1) $x^{2}+y^{2}-12 x-11=0$ 2) $x^{2}+y^{2}+4 x-21=0$ 3) $\left.x^{2}+y^{2}+12 x+11=04\right) x^{2}+y^{2}-4 x+21=0$
58. If the two circles $x^{2}+y^{2}=4$ and $x^{2}+y^{2}-24 x-10 y+a^{2}=0, a \in I$, have eactly two common tangents, then the number of possible values of ' $a$ ' is (Circles)
1) 11
2) 13
3) 0
4) 2
59. The locus of centre of a circle which passes through the origin and cuts off a length of 4 units from the line $x=3$ is
(Circles)
1) $y^{2}+6 x=13$
2) $y^{2}+6 x=0$
3) $y^{2}-6 x=13$
4) $x^{2}+6 y=13$
60. Circle $x^{2}+y^{2}+2 a x+2 b y+k=0$ bisects the circumference of $x^{2}+y^{2}+2 g x+2 f y+c=0$ then length of common chord
(System of Circles)
1) $\sqrt{g^{2}+f^{2}-c}$
2) $2 \sqrt{a^{2}+b^{2}-k}$
3) $2 \sqrt{g^{2}+f^{2}}$
4) $2 \sqrt{g^{2}+f^{2}-c}$
61. For the parabola $y^{2}+8 x-12 y+20=0$
(Parabola)
1) vertex is $(2,6)$
2) focus is $(0,6)$
3) latusrectumish $4 . A^{4}$ )axisis B' $^{6}$ ORIAL.IN
62. The sum of the distances of a point $(2,-3)$ from the foci of an ellipse $16(x-2)^{2}+25(y+3)^{2}=400$ is (Ellipse)
1) 8
2) 6
3) 50
4) 10
63. Length of the latus rectum of the hyperbola $2 x^{2}-y^{2}-4 x-4 y-20=0$.
(Hyperbola)
1) 4
2) 12
3) 7
4) 3
64. $\underset{x \rightarrow 0}{\operatorname{Lt}} \frac{x \cdot 2^{x}-x}{1-\cos x}$ is equal to
(Limits)
1) $2 \log 2$
2) $\log 2$
3) $\frac{1}{2} \log 2$
4) $\frac{1}{2}$
65. If $\underset{x \rightarrow 0}{\operatorname{Lt}} \frac{\log (3+x)-\log (3-x)}{x}=k$, the value of $k$ is
(Limits)
1) 0
2) $-\frac{1}{3}$
3) $\frac{2}{3}$
4) $-\frac{2}{3}$
66. If $\alpha$ is a repeated root of $a x^{2}+b x+c=0$, then $\underset{x \rightarrow \alpha}{\operatorname{Lt}} \frac{\tan \left(a x^{2}+b x+c\right)}{(x-\alpha)^{2}}$ is
(Limits)
1) $a$
2) $b$
3) c
4) 0
67. If $f(x)=\left\{\begin{array}{cc}\frac{x^{2}-(a+2) x+a}{x-2}, & x \neq 2 \\ 2, & x=2\end{array}\right.$ is continuous at $x=2$, then the value of $a$ is
(Continuity)
1) -6
2) 0
3) 1
4) -1
68. Let $f(x+y)=f(x) f(y)$ for all $x$ and $y$. Suppose that $f(3)=3$ and $f^{\prime}(0)=11$, then $f^{\prime}(3)$ is equal to (Differentiation)
1) 22
2) 33
3) 28
4) 30
69. The ratio of relative errors of $y$ and $x$ with respect to the given function $y=x^{n}$ is
1) $1: n$
2) $n: 1$
3) $1: 1$
4) $2: 1$
70. A variable triangle is inscribed in a circle of radius $R$. If the rate of change of a side is $R$ times the rate of change of the opposite angle then that angle is
(Rate of Change)
1) $\pi / 2$
2) $\pi / 4$
3) $\pi / 6$
4) $\pi / 3$
(Tangents \& Normals)
5) $(0,0)$
6) $\left(\frac{4}{\sqrt{3}}, 1\right)$
7) $\left(\frac{4}{\sqrt{3}}, 2\right)$
8) $\left(\frac{4}{\sqrt{3}}, \frac{11}{\sqrt{3}}\right)$
71. The point of the curve $y^{3}+3 x^{2}=12 y$. Where the tangent is vertical is
72. Rolle's theorem is applicable in the interval $[-2,2]$ for the function
(Mean Value Theorem)
1) $f(x)=x^{3}$
2) $f(x)=4 x^{4}$
3) $f(x)=2 x^{3}+3$
4) $f(x)=\pi|x|$
73. The ratio of two parts of a number 'a' such that the product of $5^{\text {th }}$ power of one and $6^{\text {th }}$ power of the other is maximum is
(Maxima \& Minima)
1) $25: 36$
2) $6: 11$
3) $5: 11$
4) $5: 6$
74. $\int \frac{\cot x}{\sqrt{\sin x}} d x$ is equal to
1) $2 \sqrt{\sin x}+c$
2) $\frac{1}{2 \sqrt{\sin x}}+c$
3) $\frac{-2}{\sqrt{\sin x}}+c$
4) $\frac{2}{\sqrt{\sin x}}+c$
75. $\int_{0}^{\frac{\pi}{2}}\left(2 \operatorname{Tan} \frac{x}{2}+x \sec ^{2} \frac{x}{2}\right) d x=$
(Definite Integrals)
1) $\pi$
2) $\pi / 2$
3) $2 \pi / 3$
4) $\pi / 6$
76. $a_{n}=\int_{\pi / 4}^{\pi / 2} \cot ^{n} x d x$, then $a_{2}+a_{4}, a_{3}+a_{5}, a_{4}+a_{6}$ are in
(Definite Integrals)
1) GP
2) $A P$
3) HP
4)AGP
77. $\underset{n \rightarrow \infty}{\operatorname{Lt}}\left[\frac{\sqrt{n^{2}-1^{2}}}{n^{2}}+\frac{\sqrt{n^{2}-2^{2}}}{n^{2}}+\frac{\sqrt{n^{2}-3^{2}}}{n^{2}}+\ldots \ldots . . n\right.$ terms $]$
(Definite Integrals)
1) $\frac{\pi}{4}$
2) $\frac{\pi}{2}$
3) $\frac{\pi}{3}$
4) $\frac{\pi}{6}$
78. The differential equation of family of parabolas with foci at the origin and axis along the $x$-axis is
1) $y\left(\frac{d y}{d x}\right)^{2}+2 x \frac{d y}{d x}-y=0$
2) $x\left(\frac{d y}{d x}\right)^{2}+2 y \frac{d y}{d x}-y=0$
(Differentiation Equatons)
3) $y\left(\frac{d y}{d x}\right)^{2}+2 x \frac{d y}{d x}+y=0$
4) $x\left(\frac{d y}{d x}\right)^{2}-2 x \frac{d y}{d x}+y=0$
79. Soltuion of the differential equation $x \sin \frac{y}{x} d y=\left(y \sin \frac{y}{x}-x\right) d x$ is
(Differentiation Equatons)
1) $\log x=\cos \left(\frac{y}{x}\right)+C$
2) $\log y=\cos \left(\frac{x}{y}\right)+C$
3) $\log x=\cos \left(\frac{x}{y}\right)+C$
4) $\log y=\cos \left(\frac{y}{x}\right)+C$
80. The solution of $\left(x^{2}-y^{2}\right) d x+2 x y d y=0$ is (Differentiation Equatons)
1) $x^{2}-y^{2}=c x$
2) $x^{2}+y^{2}=c y$
3) $x^{2}+y^{2}=c x$
4) $x^{2}-y^{2}=c y$
