

## LAQ'S (8 MARKS)

### WAVES

1. Explain the formation of stationary waves in stretched strings and hence deduce the laws of transverse waves in stretched strings.

**A. Stationary wave:** The interference of two identical waves moving in opposite directions produces stationary waves.

It forms nodes when the displacement is 0 and antinodes when the displacement is maximum

$$y_1 = A \sin(\omega t - kx)$$

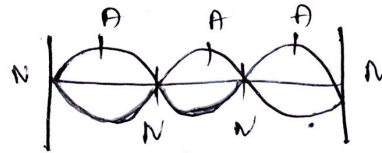
$$y_2 = A \sin(\omega t + kx)$$

$$y = y_1 + y_2$$

$$y = A \sin(\omega t - kx) + A \sin(\omega t + kx)$$

$$y = 2A \sin kx \cos \omega t$$

$$y = a_m \cos \omega t, \quad a_m = 2a \sin kx$$



- It forms alternate nodes and antinodes.
- If amplitude is zero, it gives node.
- If amplitude is maximum it gives antinode.
- The distance between N-N (or) A-A =  $\lambda/2$ .
- The distance between A-N (or) N-A =  $\lambda/4$ .
- The position of nodes  $kx = n\pi$  ( $n = 0, 1, 2, \dots$ )
- The position of antinode  $kx = \left(n + \frac{1}{2}\right)\pi$  ( $n = 0, 1, 2, \dots$ )

#### Modes of Vibration in a stretched string:

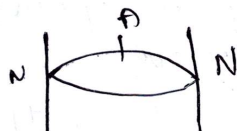
- We know that velocity of transverse wave in a stretched string is  $\sqrt{\frac{T}{\mu}}$

#### Fundamental Frequency:

- It is the lowest possible natural frequency of stationary wave is called fundamental frequency or first harmonic.

$$n_1 = \sqrt{\frac{T}{\mu}}$$

$$= v/\lambda$$



$$n_1 = \frac{v}{\lambda}$$

$$\ell = \lambda/2$$

$$n_1 = \frac{1}{2} \sqrt{\frac{T}{\mu}}$$

$$\lambda = 2\ell$$

$$n_1 = \frac{1}{2\ell} \sqrt{\frac{T}{\mu}}$$

#### First overtone:

- If the frequency is more than fundamental frequency are called overtone.

$$n_2 = \frac{1}{2} \sqrt{\frac{T}{\mu}}$$

$$n_2 = 2 \frac{1}{2\ell} \sqrt{\frac{T}{\mu}}$$

$$\ell = 2\lambda/2$$

$$\lambda = 2\ell/2$$

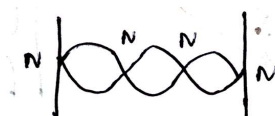


**Second Overtone:**

$$n_3 = 3 \left[ \frac{1}{2\ell} \sqrt{\frac{7}{\mu}} \right]$$

$$n_1 : n_2 : n_3 = 1 : 2 : 3$$

$$\ell = 3\lambda/2$$



**Law of Transverse wave in a Stretched String:**

$$n = \frac{1}{2\ell} \sqrt{\frac{T}{\mu}}$$

I Law :  $n \propto \frac{1}{\ell}$  [  $T$  &  $\mu$  are constant]

$$n_1 \ell_1 = n_2 \ell_2$$

II Law :  $n \propto \sqrt{T}$

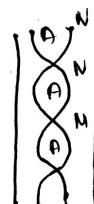
$$\frac{n_1}{n_2} = \sqrt{\frac{T_1}{T_2}} \quad [\ell \text{ & } \mu \text{ are constant}]$$

III Law :  $n \propto \frac{1}{\sqrt{\mu}}$

$$n_1 \sqrt{\mu_1} = n_2 \sqrt{\mu_2} \quad [\ell \text{ & } T \text{ are constant}]$$

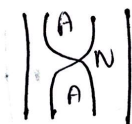
2. Explain the formation of stationary waves in an air column unclosed in open pipe. Derive the equation for the frequencies of the harmonics produced.

- A. If the pipe is open at both the ends is called open pipe.  
 $n = V/\lambda$



**Fundamental Frequency :**

$$n_1 = \frac{V}{2\ell}$$

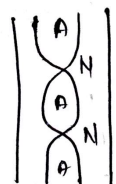


$$\ell = \lambda / 2$$

$$\lambda = 2\ell$$

**First overtone :**

$$n_2 = \frac{V}{2\ell}$$



$$\ell = 2\lambda / 2$$

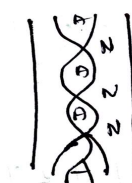
$$\lambda = 2\ell / 2$$

$$n_2 = \frac{2V}{2\ell}$$

$$\therefore n_2 = 2n_1$$

**Second overtone:**

$$n_3 = \frac{V}{2\ell}$$



$$\ell = \frac{3\lambda}{2}$$

$$\lambda = \frac{2\ell}{3}$$

$$n_3 = \frac{3V}{2\ell}$$

$$n_3 = 3n_1$$

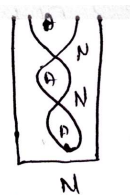
$$n_1 : n_2 : n_3 = 1 : 2 : 3.$$

**3. How are stationary waves formed in closed pipes? Explain the various modes of vibrations and obtain relations for their frequencies?**

**A.** If the pipe is closed at one end is called closed pipe.

$$v = n \lambda$$

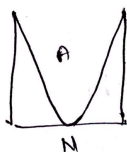
$$n = \frac{v}{\lambda}$$



**Fundamental frequency:**

It consists of one antinode and one node

$$n_1 = \frac{v}{4\ell}$$



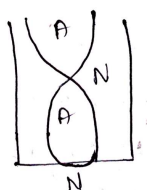
$$\ell = \frac{\lambda}{4}$$

$$\lambda = 4\ell$$

**First overtone:**

It consists of two nodes and two antinode

$$n_2 = \frac{v}{\frac{4\ell}{3}}$$



$$\ell = \frac{3\lambda}{4}$$

$$n_2 = \frac{3v}{4\ell}$$

$$\lambda = \frac{4\ell}{3}$$

$$n_2 = 3n_1$$

**Second overtone:**

It consists of three antinode and three nodes

$$n_3 = \frac{v}{\frac{4\ell}{5}}$$



$$\ell = \frac{5\lambda}{4}$$

$$n_3 = 5n_1$$

$$\lambda = \frac{4\ell}{5}$$

$$n_1 : n_2 : n_3 = 1 : 3 : 5.$$

**4. What is Doppler effect? Obtain an expression for the apparent frequency of sound heard when the source is in motion with respect to an observer at rest.**

**A.** Doppler Effect : The apparent change in the frequency due to relative motion between the source and observer is called Doppler effect.

Expression : When the source 's' is moving away from stationary observer.

Let the source produce at crest and it reaches the observer in  $t_1$  sec.

$$t_1 = \frac{L}{v} \text{ ----- (1)}$$

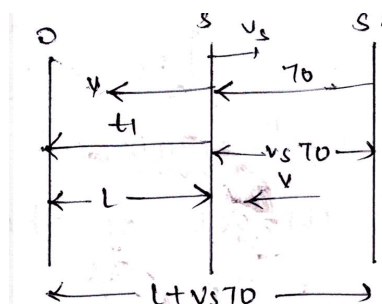
→ Now the source moved from 's' to 's'' in  $t_2$  sec with a velocity  $V_s$  and the second crest reaches the observer

$$t_2 = T_0 + \frac{L + V_s T_0}{v}$$

Similarly

$$t_{n+1} = nT_0 + \frac{L + nV_s T_0}{v} \text{ ----- (2)}$$

$$2 \text{ (-) } 1$$



$$t_n = t_{n+1} - t_1 = n T_0 + \cancel{\frac{\ell}{V}} + \frac{n V_s T_0}{V} - \cancel{\frac{\ell}{V}}$$

$$t_n = n T_0 \left[ 1 + \frac{V_s}{V} \right]$$

$$T' = \text{time period} = \frac{t_n}{n} = \frac{n T_0 \left[ 1 + \frac{V_s}{V} \right]}{n}$$

$$\text{Apparent frequency } n' = \frac{1}{T'}$$

$$n' = \frac{1}{T_0 \left[ 1 + \frac{V_s}{V} \right]} = n_0 \left[ 1 + \frac{V_s}{V} \right]^{-1} = n_0 \left[ 1 - \frac{V_s}{V} \right]$$

$$n' = n_0 \left[ \frac{V - V_s}{V} \right] \quad n' < n_0$$

similarly of 's' moves towards stationary observer.

$$n' = n_0 \frac{\mu_0 i_1 i_2 \ell}{2 \pi r} \quad n' > n_0$$

5. **What is Doppler Shift? Obtain an expression for the apparent frequency of sound heard when the observer is in motion with respect of a source at rest.**

A. **Doppler Shift:** The change in the frequency of sound produced and apparent frequency of sound heard by the listener is called Doppler shift.

Expression : Observer is moving towards stationary source

$$t_1 = \frac{L}{V + V_0}$$

$$t_2 = T_0 + \frac{L - V_0 T_0}{V + V_0}$$

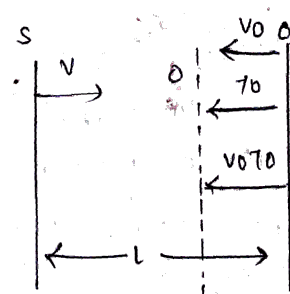
$$t_{n+1} = n T_0 + \frac{L - n V_0 T_0}{V + V_0}$$

$$T_n = t_{n+1} - t_1 = n T_0 + \cancel{\frac{L}{V + V_0}} - \frac{n V_0 T_0}{V + V_0} - \cancel{\frac{L}{V + V_0}}$$

$$T_n = n T_0 \left[ 1 + \frac{V_0}{V + V_0} \right]$$

$$T = \frac{T_n}{n} = T_0 \left[ 1 - \frac{V_0}{V + V_0} \right]$$

$$n' = \frac{1}{T} = \frac{1}{T_0 \left[ \frac{V - V_0}{V} \right]}$$



$$n' = n_0 \left[ \frac{V + V_0}{V} \right]^{-1} \quad n' > n_0$$

y (2) If 'O' is moving away from the source  $n' = n_0 \left[ \frac{V - V_0}{V} \right] \quad n' < n_0$ .

## CURRENT ELECTRICITY

6. **State Kirchhoff's Law for an electrical network using these laws deduce the condition for balance in a wheat stone bridge.**

A. **Kirchhoff's 1<sup>st</sup> Law:** The sum of the currents flowing towards a junction is equal to the sum of the current flowing away from the junction (or) the algebraic sum of current meeting at a junction is zero i.e.,  $\sum I = 0$ .

**Kirchhoff's 2<sup>nd</sup> Law:** It states that in any closed mesh of a circuit, the algebraic sum of the products of the current and resistance in each part of the loop is equal to the algebraic sum of the emf's in that loop  $\sum IR = 0$ .

**Wheatstone Bridge :** Wheatstone bridge is used to compare the resistances to determine unknown resistance and to measure small strains in hard materials. This works on the principle of Kirchhoff's laws.

**Description:** Wheatstone Bridge consists of four resistors  $R_1, R_2, R_3$  and  $R_4$  connected in the four arms of a square to form four junctions A, B, C, D as shown in the figure. A galvanometer G is connected between the junction B and D. A battery of emf and no internal resistance is connected across the junction A and C. Let G be the resistance of the galvanometer.

**Principle:** The current in the resistances are shown and let  $I_g$  be the current passing through the galvanometer. Consider the case when the current through the galvanometer is zero i.e.,  $I_g = 0$ . This is called bridge balancing condition.

By applying Kirchhoff's law to the junction B & D at junction 'B'  $I_2 = I_4 + I_g \Rightarrow I_2 = I_4$  at junction.

'D'  $I_1 + I_g = I_3 \Rightarrow I_1 = I_3$

By applying Kirchhoff's 2<sup>nd</sup> law to the closed loop ADBA

$$- I_1 R_1 + 0 + I_2 R_2 = 0$$

$$\Rightarrow I_1 R_1 = I_2 R_2 \Rightarrow \frac{I_1}{I_2} = \frac{R_2}{R_1} \text{ -----(1)}$$

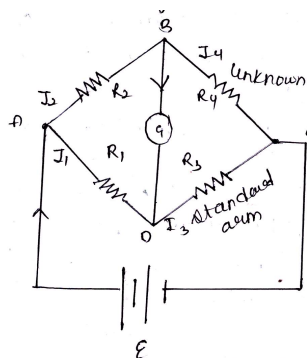
By applying Kirchhoff's 2<sup>nd</sup> law to the closed loop CBDC

$$I_2 R_4 + 0 - I_1 R_3 = 0$$

$$\Rightarrow I_2 R_4 = I_1 R_3 \Rightarrow \frac{I_1}{I_2} = \frac{R_4}{R_3} \text{ -----(2)}$$

From equation (1) and (2)  $\frac{R_2}{R_1} = \frac{R_4}{R_3}$

This is called bridge balancing condition.



7. State the working principle of potentiometer explain with the help of a circuit diagram how the emf of two primary cells are compared by using the potentiometer.

A. **Description:** A potentiometer consists of uniform wire of length 10m arranged between A and C as 10 wires each of length 1m on a wooden board.

The balancing length is measured from the end which is connected to the positive terminal of the battery by moving the Jockey J on the wire.

**Principle :**

L - Length of wire

R - Resistance of wire

Resistance of ' $\ell$ ' is  $\left(\frac{R}{L}\right)\ell$

$$I = \frac{\varepsilon}{r + R_s + R}$$

Potential across ' $\ell$ '

$V = I \times \text{resistance}$

$$V = \frac{\varepsilon}{r + R_s + R} \left[ \frac{R}{L} \right] \ell$$

$$V = \phi \ell$$

$$\phi = \frac{V}{\ell} = \text{Potential}$$

$$V \propto \ell$$

**To compare e.m.f of cells :**

$$\varepsilon = \phi \ell_1$$

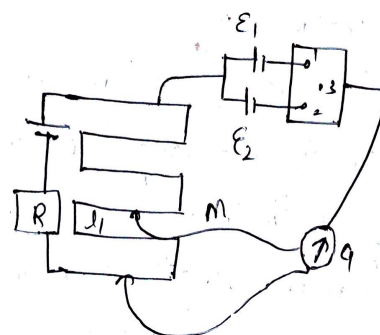
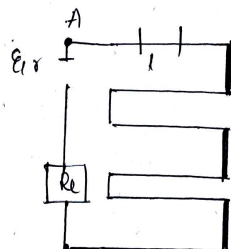
$$\varepsilon_1 \propto \ell_1$$

$$\varepsilon_2 \propto \ell_2$$

$$\frac{\varepsilon_1}{\varepsilon_2} = \frac{\ell_1}{\ell_2}$$

**Precautions :**

1. Jockey should not be damaged.
2. Current value should be small.
3. Current should be passed only while taking the reading.



8. State the working principle of potentiometer explain with the help of a circuit diagram how the potentiometer is used to determine the internal resistance of the given primary cell.

A. **Description :** A potentiometer consists of uniform wire of length 10m arranged between A and C as 10 wires each of length 1m on a wooden board since the wire is uniform the p.d between A and any point at a distance  $\ell$  from A is  $\varepsilon(\ell) = \phi \ell$  where  $\phi$  is the potential drop per unit length of the potentiometer wire.

**Principle:**

L = Length of the wire

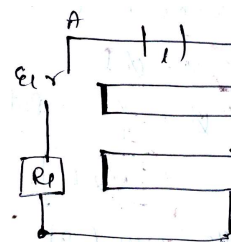
R = Resistance of wire

Resistance of " $\ell$ " is  $\left(\frac{R}{L}\right)\ell$

$$I = \frac{\varepsilon}{r + R_s + R}$$

Potential across ' $\ell$ '

$V = I \times \text{resistance}$



$$V = \frac{\varepsilon}{r + R_s + R} \left[ \frac{R}{L} \right] \ell$$

$$V = \phi \ell$$

$$\phi = \frac{V}{\ell} = \text{Potential}$$

$$V \propto \ell$$

**Inter resistance (r) :**

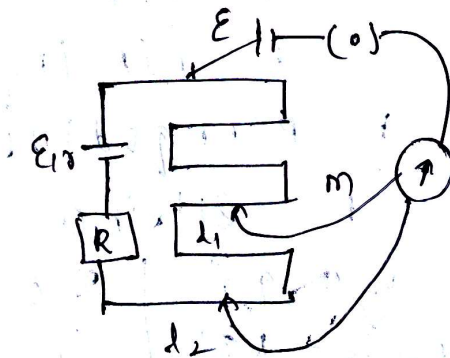
$$\varepsilon_1 \propto \ell_1$$

$$V \propto \ell_2$$

$$\frac{\varepsilon}{V} = \frac{\ell_1}{\ell_2}$$

$$\frac{\ell_1}{\ell_2} - 1 = \frac{r}{R} \Rightarrow \frac{r}{R} = \frac{\ell_1 - \ell_2}{\ell_2}$$

$$r = R \left[ \frac{\ell_1 - \ell_2}{\ell_2} \right]$$



**Precautions:**

- 1) Jockey should not be dragged along the wire.
- 2) Current value should be small.
- 3) Current should be passed while taking readings.

## MOVING CHARGES AND MAGNETISM

9. Deduce an expression for the force on a current carrying conductor placed in a magnetic field. Derive an expression for the force per unit length between two parallel current conductors.

- A. Let us consider a conductor of length ' $\ell$ ' area of cross section ' $A$ ' placed in uniform magnetic field of induction  $\vec{B}$  as shown in the figure.

Force acting on the charge

$$\vec{F} = -q (\vec{v} \times \vec{B})$$

$$= -B_2 v \sin \theta$$

Area of conductor =  $A$

Vel of charge =  $v$

Force acting on the conductor

$$F = n \ell A f$$

$$F = n \ell A (B q v \sin \theta)$$

$$F = B (n A q v d) \ell \sin \theta$$

$$F = B i \ell \sin \theta$$

If  $\theta = 90^\circ$

If  $\theta = 0^\circ$

$f_{\text{max}} = B i \ell$

$f_{\text{min}} = 0$

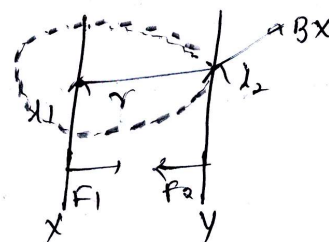
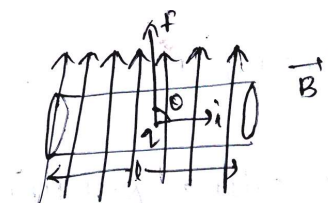
Let us consider two parallel conductors  $x$  and  $y$  separated by a distance ' $r$ ' as shown in the figure. Let  $i_1$  and  $i_2$  be the currents passing through the conductors.

$$B_x = \frac{\mu_0 i_1}{2\pi r}$$

Force acting on ' $y$ ' due to  $B_x$  is

$$F_y = B \times i_2 \ell \quad (\because \theta = 90^\circ)$$

$$F_y = \frac{\mu_0 i_1 i_2 \ell}{2\pi r}$$



similarly  $B_y = \frac{\mu_0 i_2}{2\pi r}$  and  $F_x = \frac{\mu_0 i_1 i_2 \ell}{2\pi r}$   $\therefore F_1 = F_2 = F_3 = \frac{\mu_0 i_1 i_2 \ell}{2\pi r}$

Force acting per unit length  $\frac{F}{\ell} = \frac{\mu_0 i_1 i_2}{2\pi r}$

**10. Obtain an expression for the torque on a current carrying loop placed in a uniform magnetic field. Describe the construction and working of a moving coil galvanometer.**

**A.** Let us consider a rectangular coil of length ' $\ell$ ' breadth ' $b$ ' placed in uniform magnetic field as shown in the figure.

Along the length side

(AD and BC)

$F_1 = F_2 = B i \ell$  [  $\because \theta = 90^\circ$  ]

Along AB and CD  $F_3 = F_4 = B i b$

Resultant force along

AB & CD = 0

Torque T = one of the force

X perpendicular distance (PR)

$T = B i \ell b \sin \theta$

$T = B i A \sin \theta$

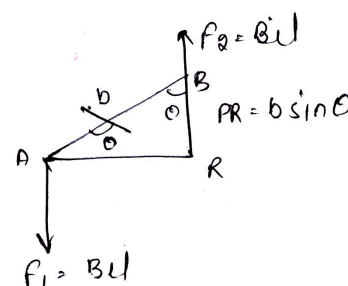
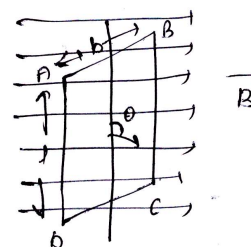
For 'N' no. of turns

If  $\theta = 90^\circ$

$T_{\max} = B i A N$

If  $\theta = 0^\circ$

$T_{\min} = 0$



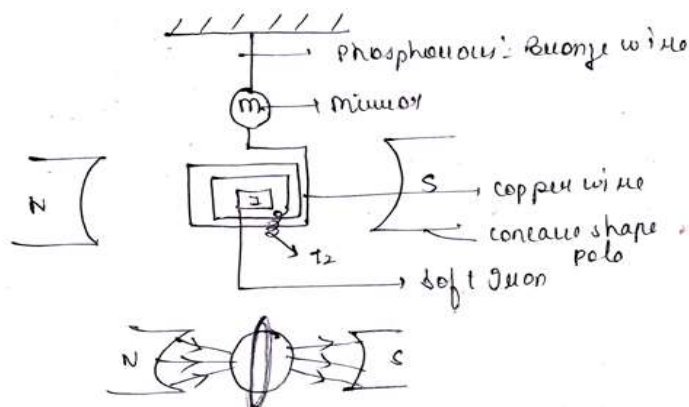
**Moving coil Galvanometer:**

Let us consider a copper wire wound on a non-metallic frame and placed in between concave shaped poles as shown in the figures.

→ Let 'm' be the mirror is used to measure the number of deflections.

→ It is used to detect and measure small electric current of the order  $10^{-9}$  amper's.

**Principle:** When a current carrying coil placed in a uniform magnetic field it experiences a torque.



In equilibrium position

Torque = Resoring couple

$B i A N = C \theta$

$i = \frac{C}{B A N} \theta$

$i = k \theta$

$i \propto \theta$



11. Explain the principle and working of a nuclear reactor with the help of a labelled diagram.

**A. Principle of Nuclear Reactor:** Nuclear reactor is used to produce a large amount of nuclear energy through a controlled nuclear fission process.

The essential part of a nuclear reactor are

i) Nuclear fuel ii) Moderator iii) Control rods iv) Protective shielding v) Coolant

i. **Nuclear Fuel :** The fissionable material used in the reactor is called nuclear fuel. The uranium isotopes  ${}_{92}\text{U}^{235}$  and  ${}_{92}\text{U}^{238}$ . Plutonium Pu and thorium  ${}_{90}\text{Th}^{232}$  are commonly used fuels in the reactors.

ii. **Moderators:** Core contain moderators. These are used to slow down the fast moving neutrons produce in the fission process. The material used as moderators are heavy water carbon in the form of pure graphite hydrocarbon plastics etc. The core is surrounded by reflectors to reduce leakage.

iii. **Control rods:** These are the materials that can absorb the neutrons and control the nuclear chain reaction cadmium or Boron or Beryllium rods are generally used for this purpose.

iv. **Protective Shielding:** It is used to prevent the spreading of radioactive effect to the space around the nuclear reactor. For this purpose lead block, concrete walls of thickness 10m is used.

v. **Coolant :** The material used to absorb heat generated in the reactor is called coolant. The coolants are water molten sodium etc.

**Working:**

i. Uranium fuels are placed in the aluminium cylinders which are separated by some distance. The graphite moderators in the form of pure carbon blocks is placed in between the fuel cylinder.

ii. To control the number of neutrons a number of control rods of cadmium or beryllium or boron are placed in the holes of graphite block.

iii. When thermal neutron collides with  $\text{U}^{235}$  nuclei it undergoes fission then produces fast neutrons are liberated. These neutrons pass through the surrounding graphite moderator and lose their kinetic energy to become thermal reaction.

iv. These thermal neutrons are captured by  $\text{U}^{235}$  which carries out the fission reaction.

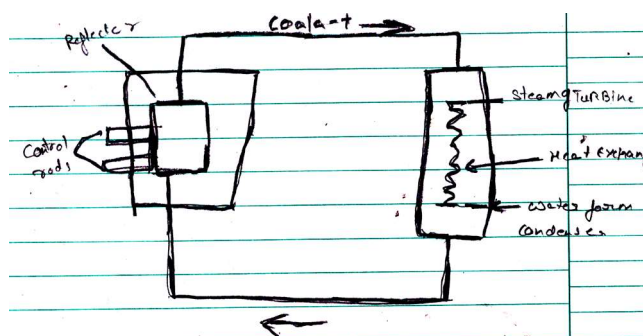
v. By using control rods the fission process can be controlled by absorbing neutrons.

vi. The steam used to rotate a turbine for the production of electric power.

**Used of nuclear reactors:**

To generate electric power.

To produce radioactive materials like plutonium -239 used in the field of medicine, industry etc.



\*\*\*\*\*The End\*\*\*\*\*